

$$(1) y = \frac{1}{e^x + 1}$$

$$(2) y = \sqrt{x^2 - 2x + 2}$$

$$(3) y = \frac{x^4 - 2x^2 + 1}{x^5}$$

$$(4) y = x^2 \log x$$

$$(5) y = 2^{\sin x}$$

(1) ~ (5) を微分せよ

微分積分 I ~~2007~~前期レポート課題 解答 2007年

$$(1) \quad y' = \frac{1' \cdot (e^x + 1) - 1 \cdot (e^x + 1)'}{(e^x + 1)^2} = \frac{0 \cdot (e^x + 1) - 1 \cdot e^x}{(e^x + 1)^2} \\ = \boxed{-\frac{e^x}{(e^x + 1)^2}}$$

$$(2) \quad u = x^2 - 2x + 2 \quad \text{と} \quad y = \sqrt{u} \quad \text{の合成関数}$$

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx} = \left(\frac{d}{du} u^{\frac{1}{2}} \right) \cdot \frac{d}{dx} (x^2 - 2x + 2) \\ = \frac{1}{2} u^{-\frac{1}{2}} \cdot (2x - 2) = \frac{x - 1}{u^{\frac{1}{2}}} = \frac{x - 1}{\sqrt{u}} \\ = \boxed{\frac{x - 1}{\sqrt{x^2 - 2x + 2}}}$$

$$(3) \quad y' = \left(\frac{1}{x} - \frac{2}{x^3} + \frac{1}{x^5} \right)' = (x^{-1} - 2x^{-3} + x^{-5})' \\ = (-1)x^{-2} - 2 \cdot (-3)x^{-4} + (-5)x^{-6} \\ = -\frac{1}{x^2} + \frac{6}{x^4} - \frac{5}{x^6} \\ = \boxed{\frac{-x^4 + 6x^2 - 5}{x^6}} \\ (= \frac{-(x^2 - 1)(x^2 - 5)}{x^6} = \frac{-(x+1)(x-1)(x+\sqrt{5})(x-\sqrt{5})}{x^6})$$

$$(4) \quad y' = (x^2)' \log x + x^2 \cdot (\log x)' \\ = 2x \log x + x^2 \cdot \frac{1}{x} \\ = 2x \log x + x = \boxed{x(2 \log x + 1)}$$

$$(5) \quad u = \sin x \quad \text{と} \quad y = 2^u \quad \text{の合成関数}$$

$$\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx} = \left(\frac{d}{du} 2^u \right) \cdot \left(\frac{d}{dx} \sin x \right) = 2^u (\log 2) \cos x \\ = \boxed{(\log 2) (\cos x) \cdot \sin x}$$